

# Modulation Instability and Tunable Raman Gain in Mid-IR Waveguides

**Pablo Fierens**

CONICET

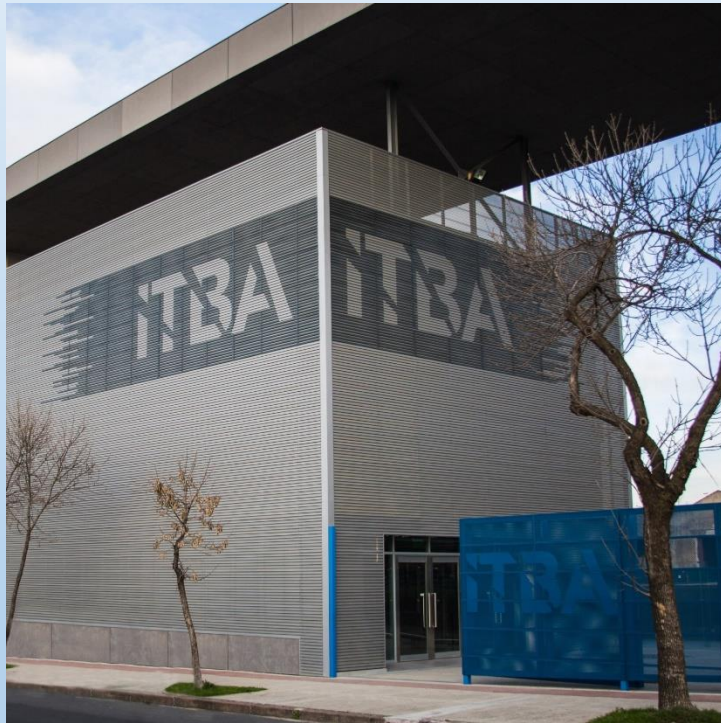


**ITBA**

Instituto Tecnológico  
de Buenos Aires

# Our group

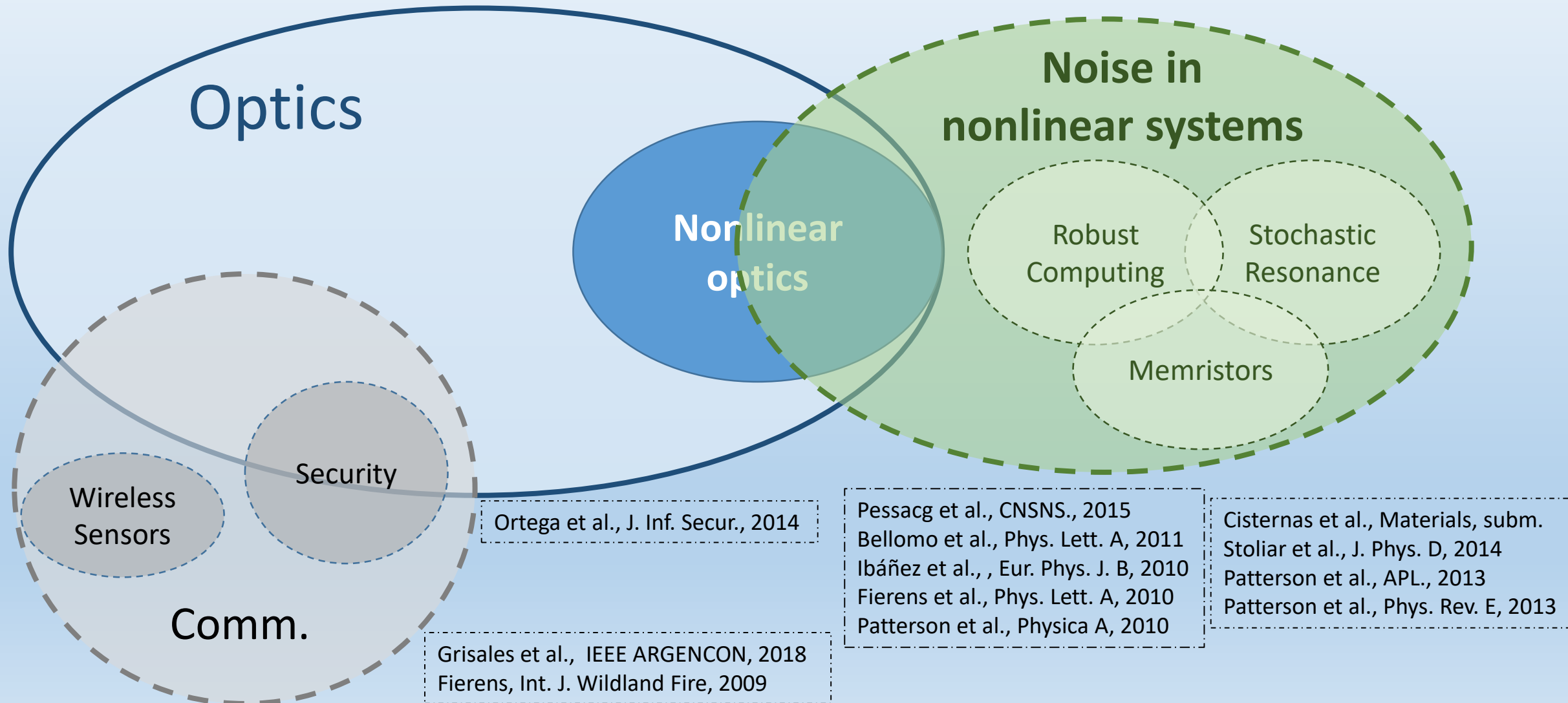
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- Instituto Tecnológico de Buenos Aires
  - Private university
  - ~ 3500 students
  - Focus on engineering
  - 3 PhD programs
  - Several graduate programs
  - 10 undergrad degrees

# Our group

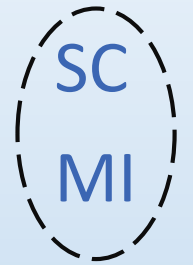
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# Light sources in the mid-IR

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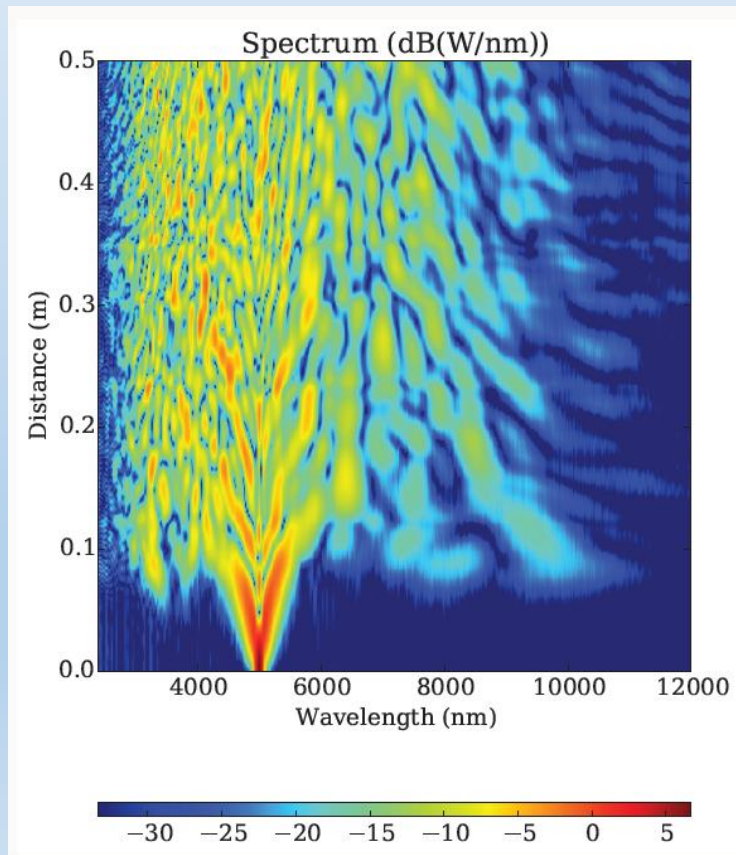
- Molecular fingerprint region
- Need for broadband and intense light sources
  - A common approach: supercontinuum generation (SC)
    - ✓ CO<sub>2</sub> laser as pump (10 μm, 5 μm from SHG) on a chalcogenide waveguide?
- Correlated photon pairs in the atmospheric windows (3-4 and 8-12 μm) for quantum information transmission
  - ✓ Parametric processes of sum/difference of frequencies in crystals (GaSe, AgGaSe<sub>2</sub>) with second order nonlinear susceptibility  $\chi_2$ ?



This talk

# Nonlinear optics

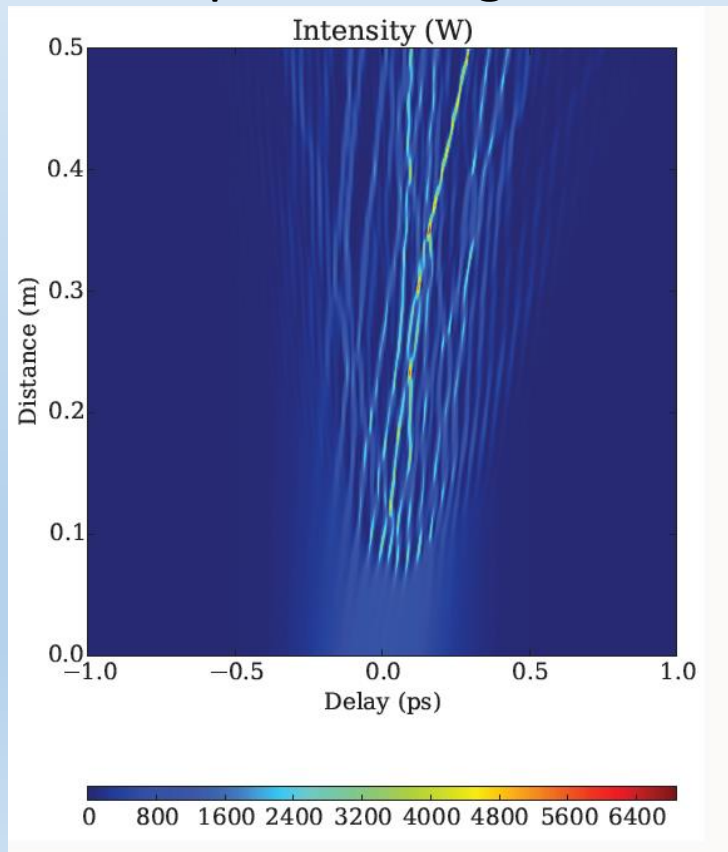
- What are we interested in?
  - Supercontinuum generation in the mid IR (Dudley, Genty & Coen, Rev. Mod. Phys, 2006)



- ✓ Simulation: 200 fs pump pulse + noise
- ✓ Chalcogenide glass fiber
- ✓  $P_0 = 1$  kW,  $\lambda_0 = 5$   $\mu$ m

# Nonlinear optics

- What are we interested in?
  - Intense pulses - rogue waves (Solli et al., Nature, 2007)



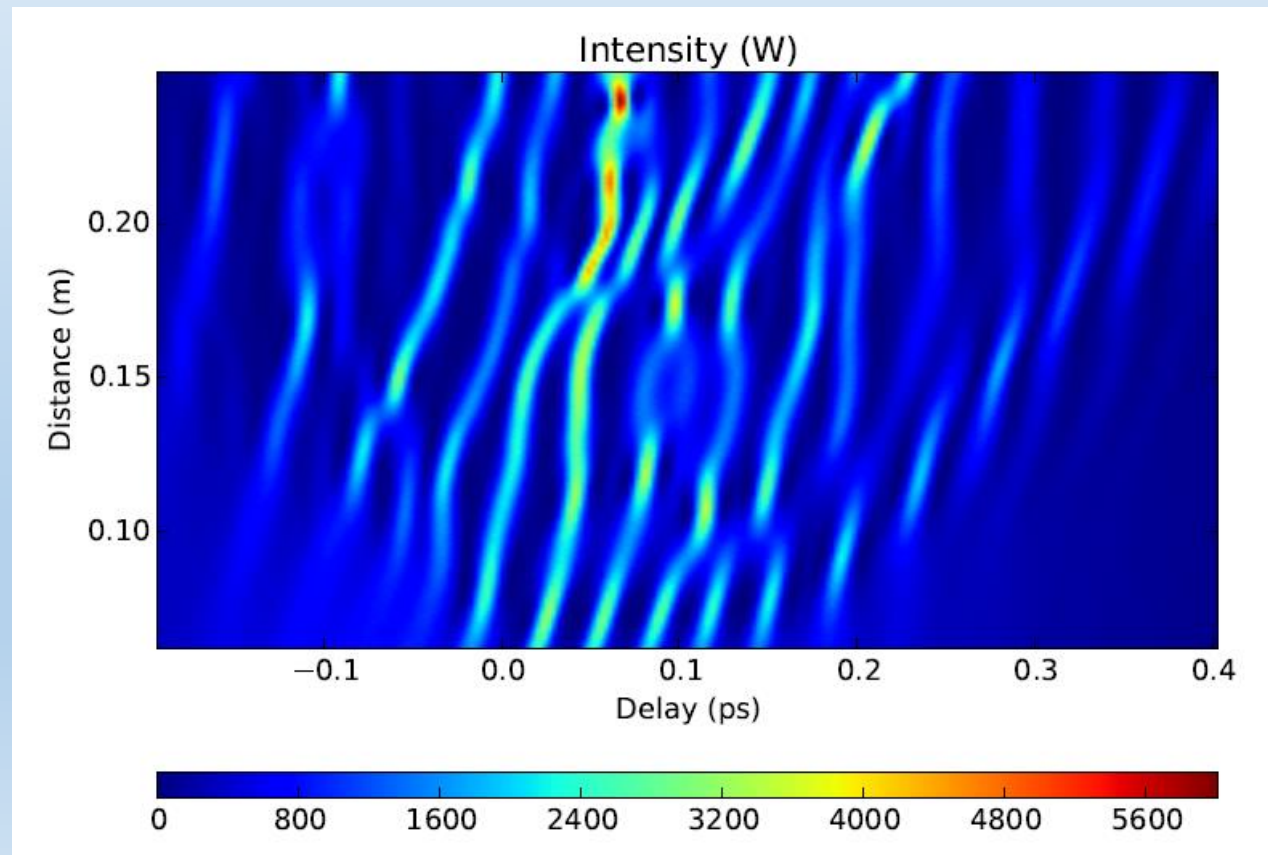
- ✓ Simulation: 200 fs pump pulse + noise
- ✓ Chalcogenide glass fiber
- ✓  $P_0 = 1$  kW,  $\lambda_0 = 5$   $\mu$ m

Grosz et al., EECOS 2015

# Nonlinear optics

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- What are we interested in?
  - Intense pulses - rogue waves



# Nonlinear optics

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- What are we interested in?
  - Supercontinuum generation in the mid IR
  - Intense pulses - rogue waves
  - Parametric amplification (Stolen & Bjorkholm, IEEE J. Quantum Electron., 1982)



# Nonlinear optics

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- What are we interested in?

- Supercontinuum generation in the mid IR
- Intense pulses - rogue waves
- Parametric amplification

Modulation instability



breaks up into pulses ← propagation of a CW in an optical fiber is unstable

Benjamin & Feir, J. Fluid Mech., 1967

Shabat & Zakharov, JETP, 1972

Akhmediev & Korneeov, Theor. Math. Phys, 1986

Tai, Hasegawa & Tomita, PRL, 1986

Potasek, Optics Lett., 1987

# Modulation instability

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- 40 years of research! Should I end my talk now?
  - Most of the analyses of MI do not include all details relevant to optical fibers.
    - ✓ One exception: Bédot et al., Phys. Rev. A, 2011
  - Not a lot of work on (quasi-)analytical approaches to the interaction of noise and nonlinearity in MI
- Coming next...
  - A complete analysis of the spectral evolution of a perturbation to a CW
  - Analytical results on input noise + MI

# Propagation in optical fibers

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- Generalized Nonlinear Schrödinger Equation (GNLSE)

$$\frac{\partial A}{\partial z} - i\hat{\beta}A = i\hat{\gamma}A(z, T) \int_{-\infty}^{+\infty} R(T') |A(z, T - T')|^2 dT'$$

- Dispersion 
$$\hat{\beta} = \sum_{m \geq 2} \frac{i^m}{m!} \beta_m \frac{\partial^m}{\partial T^m}$$

- Nonlinearity 
$$\hat{\gamma} = \sum_{n \geq 0} \frac{i^n}{n!} \gamma_n \frac{\partial^n}{\partial T^n}$$

- Raman scattering 
$$R(T) = (1 - f_R)\delta(T) + f_R h(T)$$

# Perturbation to the stationary solution

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$$A(z, T) = (\sqrt{P_0} + a)e^{i\gamma_0 P_0 z} = A_s + ae^{i\gamma_0 P_0 z}$$

- Input power:  $P_0$
- Perturbation:  $a(z; T)$

- Linear terms in the frequency domain

$$\frac{\partial \tilde{a}(z, \Omega)}{\partial z} + \tilde{N}(\Omega)\tilde{a}(z, \Omega) = \tilde{M}(\Omega)\tilde{a}^*(z, -\Omega)$$

- Frequency:  $\Omega = \omega - \omega_0$
- $\tilde{N}(\Omega) = -i \left[ \tilde{\beta}(\Omega) + P_0 \tilde{\gamma}(\Omega) (1 + \tilde{R}(\Omega)) - P_0 \gamma_0 \right]$
- $\tilde{M}(\Omega) = iP_0 \tilde{\gamma}(\Omega) \tilde{R}(\Omega)$

# Perturbation to the stationary solution

---

$$\frac{\partial \tilde{a}(z, \Omega)}{\partial z} + \tilde{N}(\Omega) \tilde{a}(z, \Omega) = \tilde{M}(\Omega) \tilde{a}^*(z, -\Omega)$$

- Ansatz:  $a(z, \Omega) = D \exp(iK(\Omega)z)$



$$K(\Omega) = -\tilde{B}(\Omega) \pm K_D(\Omega) = -\tilde{B}(\Omega) \pm \sqrt{\tilde{B}^2(\Omega) - \tilde{C}(\Omega)}$$

- $\tilde{B}(\Omega)$  and  $\tilde{C}(\Omega)$  are complex functions of the parameters
- Agrees with B ejot et al., Phys. Rev. A, 2011

Fierens et al., ICAND 2016  
Bonetti et al., Phys. Rev. A, 2016

# Modulation instability gain

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- Only self-steepening:  $\gamma_1 = \gamma_0 \tau_{sh}$ ,  $\gamma_n = 0$  for  $n \geq 2$

$$K(\Omega) = \widetilde{\beta}_o + P_0 \gamma_0 \tau_{sh} \Omega (1 + \widetilde{R}) \pm \sqrt{(\widetilde{\beta}_e + 2\gamma_0 P_0 \widetilde{R}) \widetilde{\beta}_e + P_0^2 \gamma_0^2 \tau_{sh}^2 \Omega^2 \widetilde{R}^2}$$

- Well-known facts about MI gain =  $2\text{Im}\{K(\Omega)\}$ :
  - It does not depend on odd terms of the dispersion relation
  - Self-steepening enables a gain even in a zero-dispersion fiber
  - In the large power limit, it is independent of the dispersion and it is dominated by Raman:

$$|g(\Omega)| \approx 2P_0 \gamma_0 \tau_{sh} |\Omega| \cdot |\text{Im}\{\widetilde{R}(\Omega)\}|$$

# Spectral evolution

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$$\begin{aligned} & \tilde{a}(z, \Omega) \\ &= \frac{e^{-i\tilde{B}(\Omega)z}}{K_D(\Omega)} \cdot \tilde{M}(\Omega) \sin(K_D(\Omega)z) \tilde{a}^*(0, -\Omega) + \frac{e^{-i\tilde{B}(\Omega)z}}{K_D(\Omega)} \\ & \cdot \left[ K_D(\Omega) \cos(K_D(\Omega)z) - \left( \tilde{N}(\Omega) - i\tilde{B}(\Omega) \right) \sin(K_D(\Omega)z) \right] \tilde{a}(0, \Omega) \end{aligned}$$

- Interaction between  $\tilde{a}(z, \Omega)$  and  $\tilde{a}(z, -\Omega)$  due to the nonlinearity
- $a(0, T) \in \mathbb{R} \implies \tilde{a}(z, \Omega) = \tilde{H}(\Omega, z)\Lambda(\Omega)$

# Noise-only

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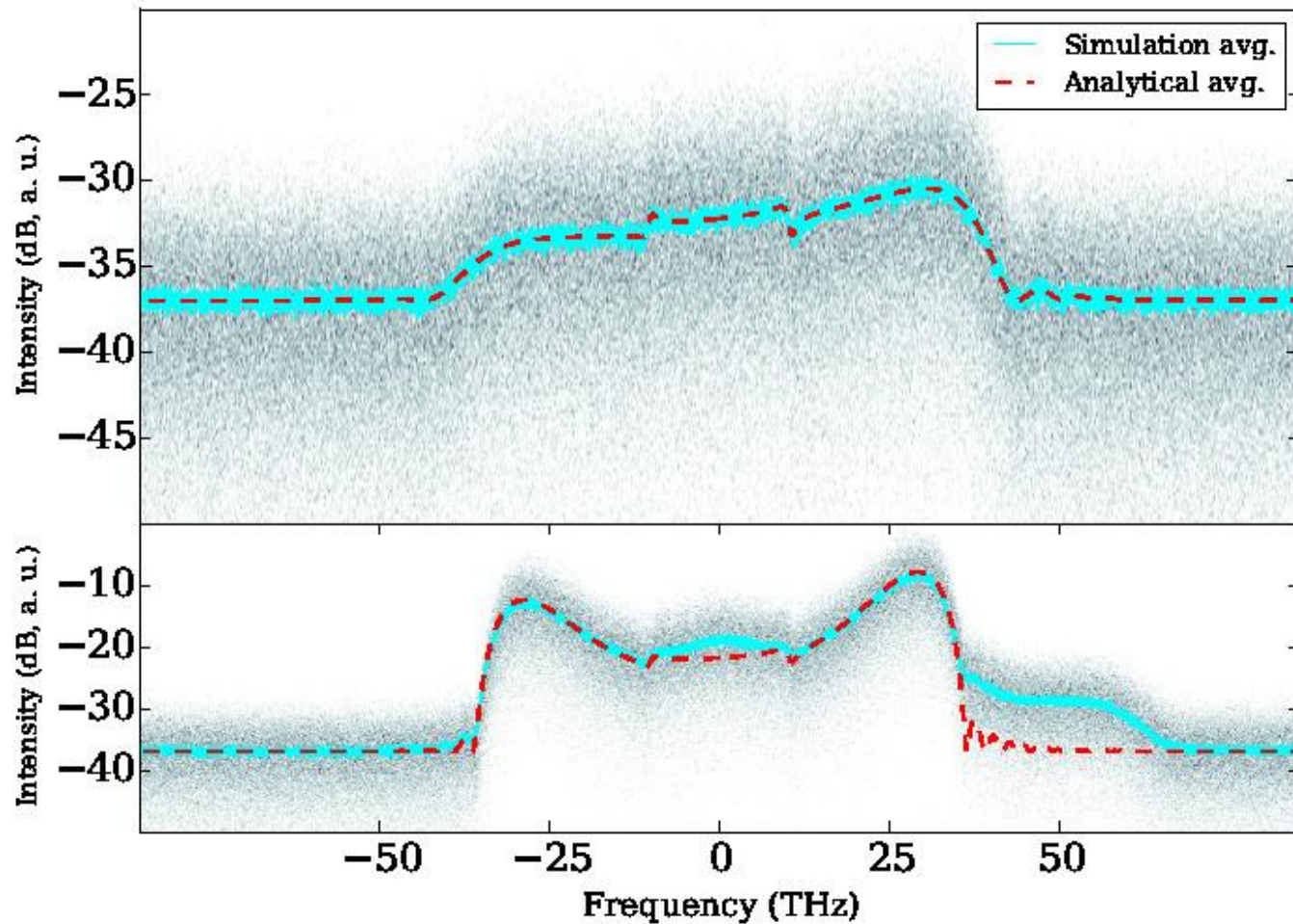
$$\tilde{a}(0, \Omega) \sim \mathcal{CN}(0, \sigma^2) \rightarrow \tilde{a}(z, \Omega) \sim \mathcal{CN}(0, \sigma_{\tilde{a}}^2)$$

$$\rightarrow |\tilde{a}(z, \Omega)| \sim \text{Rayleigh}(\sigma_{\tilde{a}}) \rightarrow |\tilde{a}(z, \Omega)|^2 / \sigma_{\tilde{a}}^2 \sim \chi_2^2$$

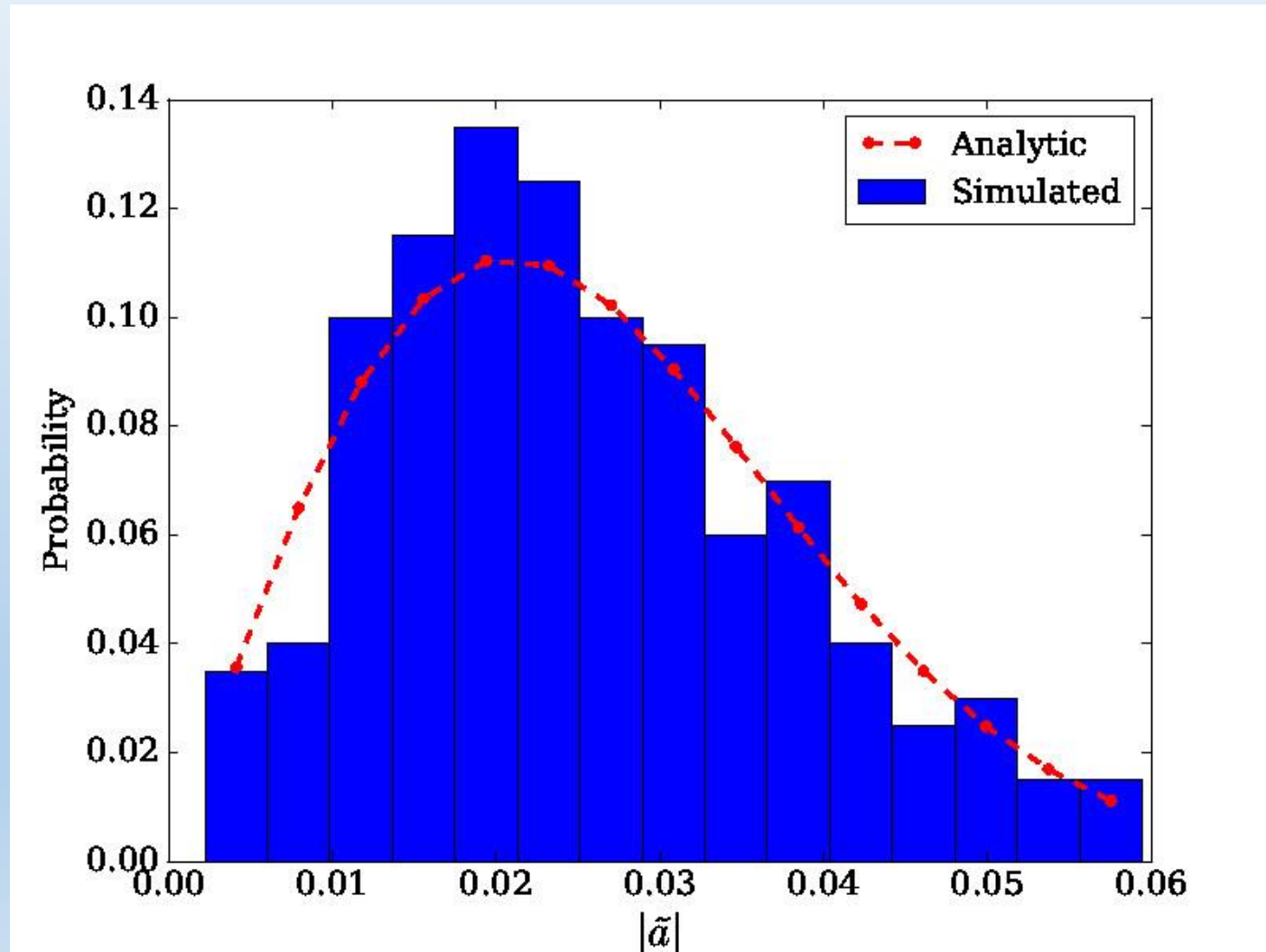
- $\sigma_{\tilde{a}}^2(z, \Omega)$  can be easily computed from previous equations



# Noise-only



# Noise-only



# Noisy input

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- A more interesting case: additive white Gaussian noise

$$a(0, \Omega) = \tilde{s}(\Omega) + \eta(\Omega), \quad \eta(\Omega) \sim \mathcal{CN}(0, \sigma_a^2)$$

- Relevant for controlling the generation of rogue waves
  - Solli, Ropers & Jalali, PRL, 2008
  - Dudley, Genty & Eggleton, Opt. Express, 2008
  - Sørensen et al., JOSA B, 2012
- We developed analytical expressions for some relevant metrics of the resulting spectrum

# Noisy input

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- Coherence (Dudley, Genty & Coen, Phys. Rev. Mod., 2006)

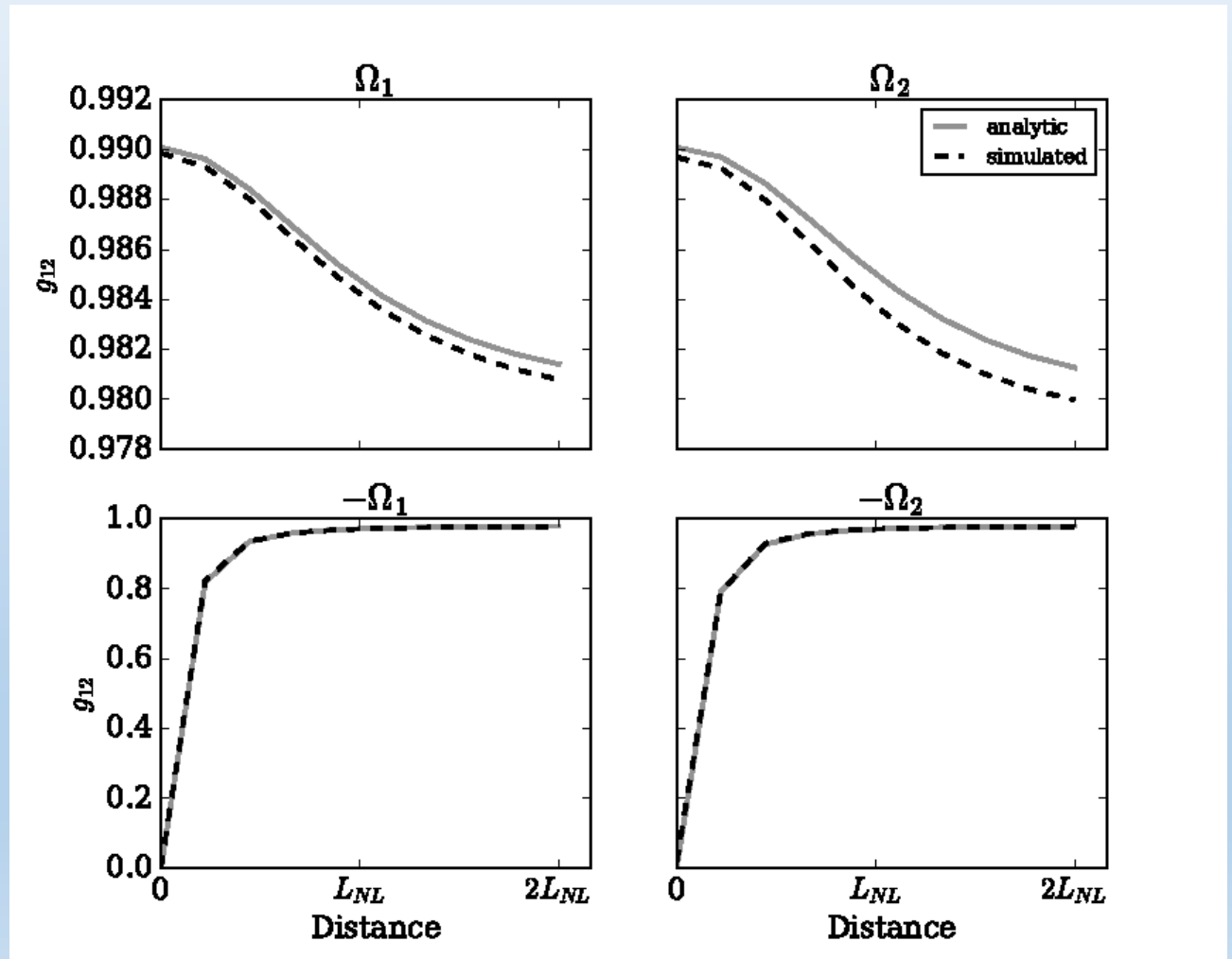
$$g_{12}(z, \Omega) = \frac{\langle \widetilde{a}_k^*(z, \Omega) \widetilde{a}_l(z, \Omega) \rangle_{k \neq l}}{\sqrt{\langle |\widetilde{a}_k(z, \Omega)|^2 \rangle \langle |\widetilde{a}_l(z, \Omega)|^2 \rangle}}$$

- Characterizes shot-to-shot fluctuations in the phase of supercontinuum spectra

# Noisy input

- Coherence

- ✓ Standard Single Mode Fiber (SSMF)
- ✓ 1 W pump at 1550 nm
- ✓ 1 mW power seeds at 31 and 46 GHz



# Noisy input

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- A simple case:
  - One-sided seed,  $\tilde{s}(\Omega) = 0$  for  $\Omega < 0$
  - No self-steepening and no Raman
- Small  $z$

$$g_{12}(z, \Omega) \approx 1 - \left(1 + \left(\frac{z}{L_{NL}}\right)^2\right) \frac{\sigma^2}{|\tilde{s}(|\Omega|)|^2} \quad \Omega > 0$$

$$g_{12}(z, \Omega) \approx 1 - \left(2 + \left(\frac{L_{NL}}{z}\right)^2\right) \frac{\sigma^2}{|\tilde{s}(|\Omega|)|^2} \quad \Omega < 0$$

- Large  $z$

$$g_{12}(z, \Omega) \approx 1 - 2 \frac{\sigma^2}{|\tilde{s}(|\Omega|)|^2}$$

# Modulation instability

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- Analytical expressions for the spectral evolution of a perturbation to a continuous pump propagating in an optical fiber, including all relevant details
- Analytical results for some metrics of supercontinuum generation, such as coherence, for noisy inputs
- Problems:
  - Undepleted pump  $\Rightarrow$  valid for short distances
  - Disregards cascading four-wave mixing effect

# Higher-order perturbation

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- The analysis can be extended to higher-order perturbation

Bonetti et al., ICAND 2018

Bonetti et al., Comm. Nonlinear Sci. Numer. Simulat., 2019

- If  $\langle |\tilde{a}(0, \Omega)|^2 \rangle = s$ , the first order solution can be written as

$$\langle |\tilde{a}_1(z, \Omega)|^2 \rangle \approx s + (e^{2g(\Omega)z} - 1)|A_1(\Omega)|^2 s$$

- This first order solution motivates the ansatz

$$\tilde{a}(z, \Omega) \approx \sqrt{s} e^{i\phi_0(z, \Omega)} + \sum_{n=1}^{\infty} (e^{G_n(\Omega)z} - 1) A_n(\Omega) \sqrt{s^n} e^{i\phi_n(z, \Omega)}$$



# Higher-order perturbation

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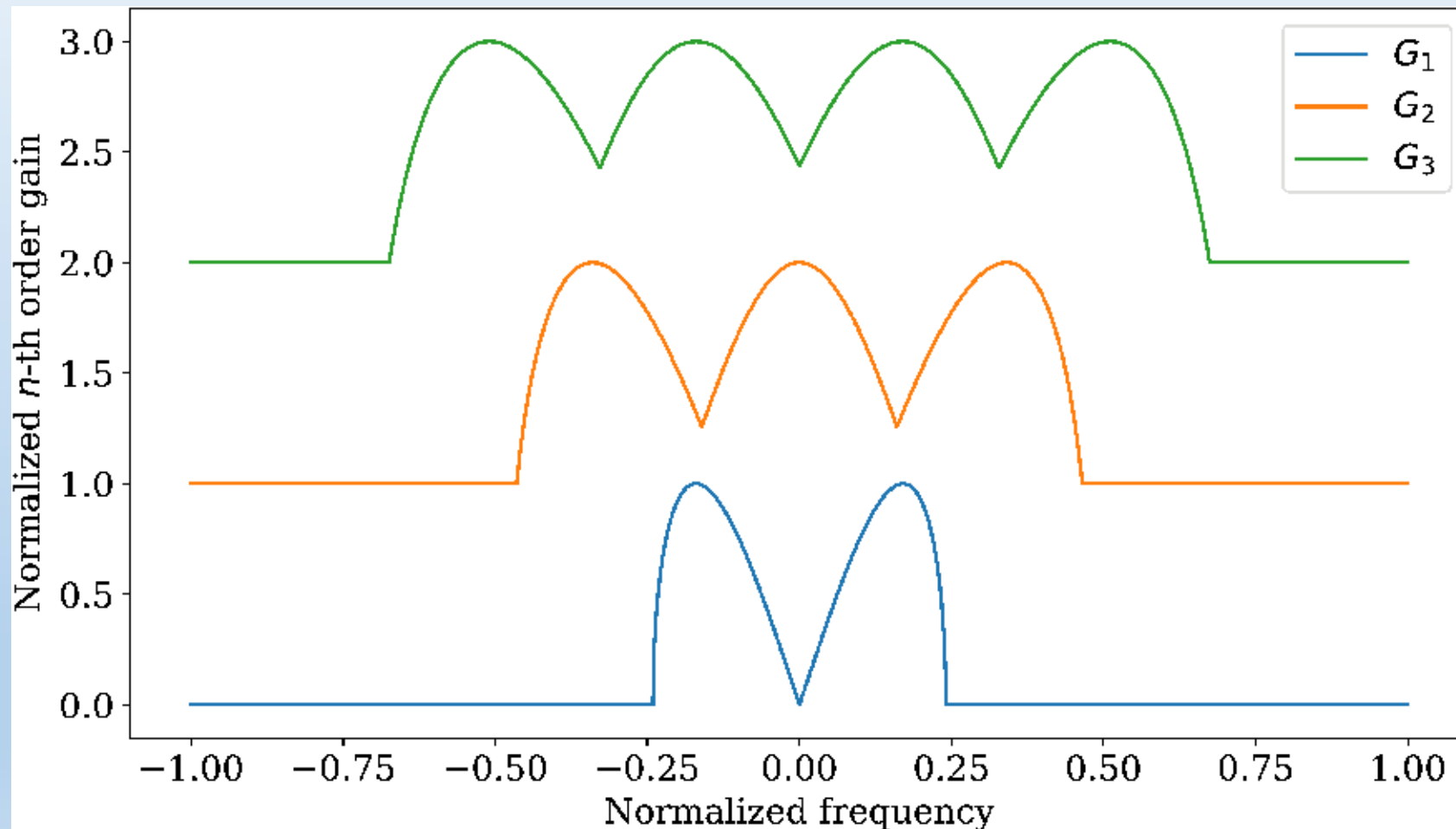
- After some lengthy manipulations, we arrive at the following expressions:

$$G_n(\Omega) = \max_u G_1(u) + G_{n-1}(u - \Omega)$$

$$\langle |A_n(\Omega)|^2 \rangle = \frac{\alpha^{n-1} \widetilde{\gamma}^2(\Omega) \left[ |\widetilde{B}(-\Omega) - iG_n(\Omega)|^2 + \widetilde{\gamma}^2(-\Omega) \right]}{\left| \left( \widetilde{B}(\Omega) + iG_n(\Omega) \right) \left( \widetilde{B}(\Omega) - iG_n(\Omega) \right) - \widetilde{\gamma}(\Omega) \widetilde{\gamma}(-\Omega) \right|^2}$$

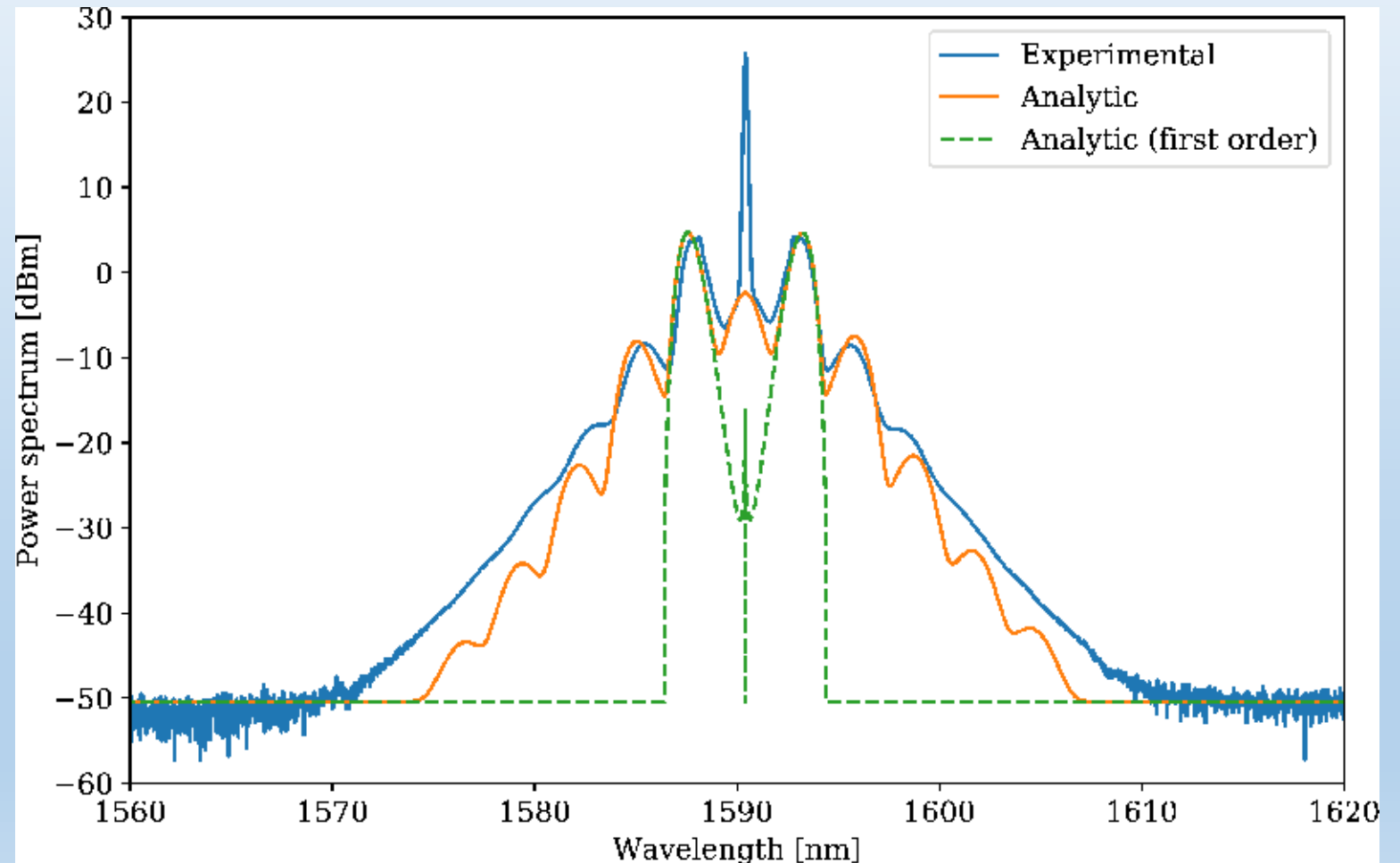
- The first equation describes the cascading effect of four-wave mixing

# Higher-order perturbation



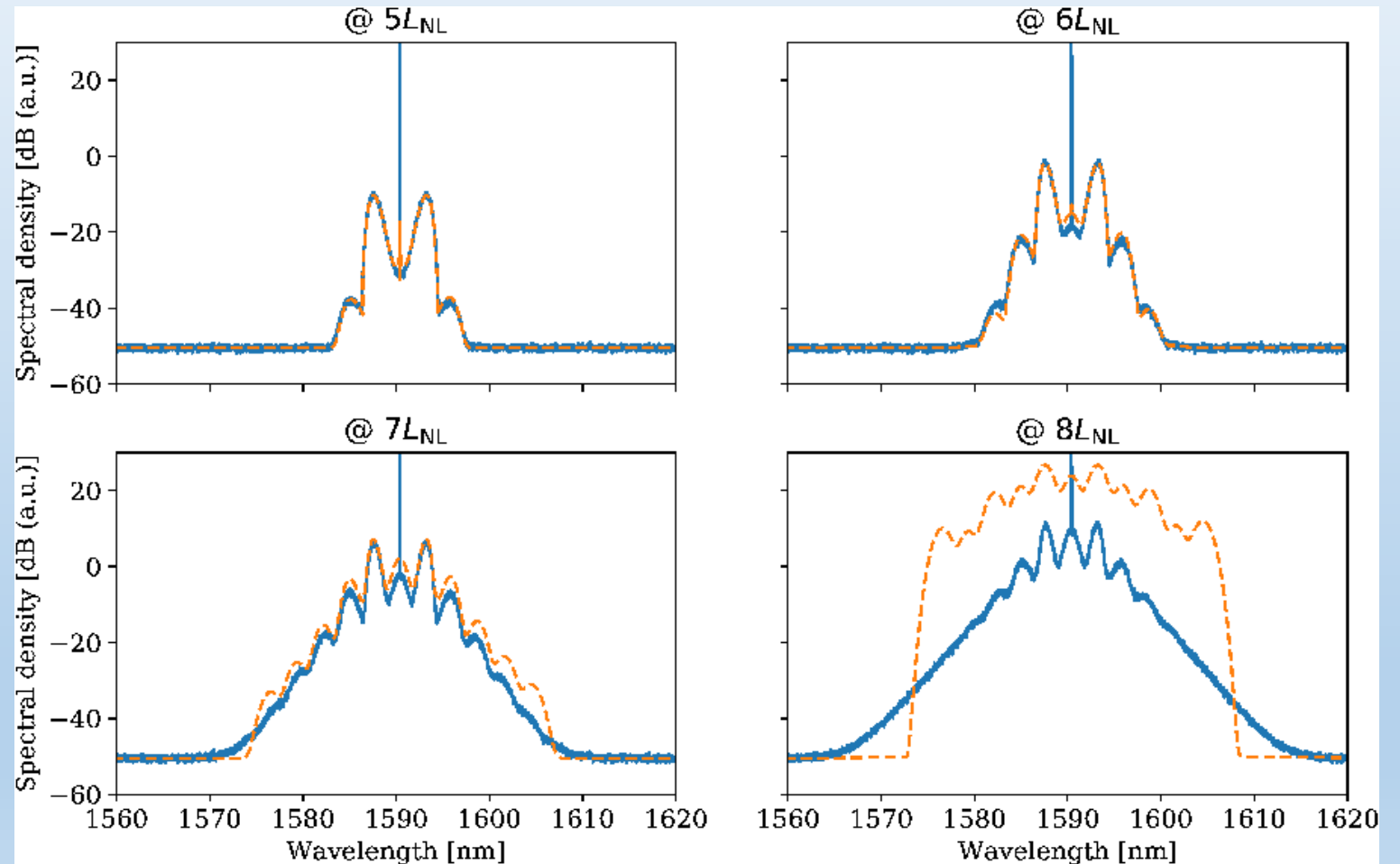
# Higher-order perturbation

- ✓ 770 m-long, dispersion-stabilized Highly-Nonlinear Fiber (HNLF)
- ✓ CW 30-dBm pump laser at 1590.4 nm



# Higher-order perturbation

- ✓ Dispersion-stabilized Highly-Nonlinear Fiber (HNLF)
- ✓ CW 30-dBm pump laser at 1590.4 nm



# Modulation instability: Power cutoff

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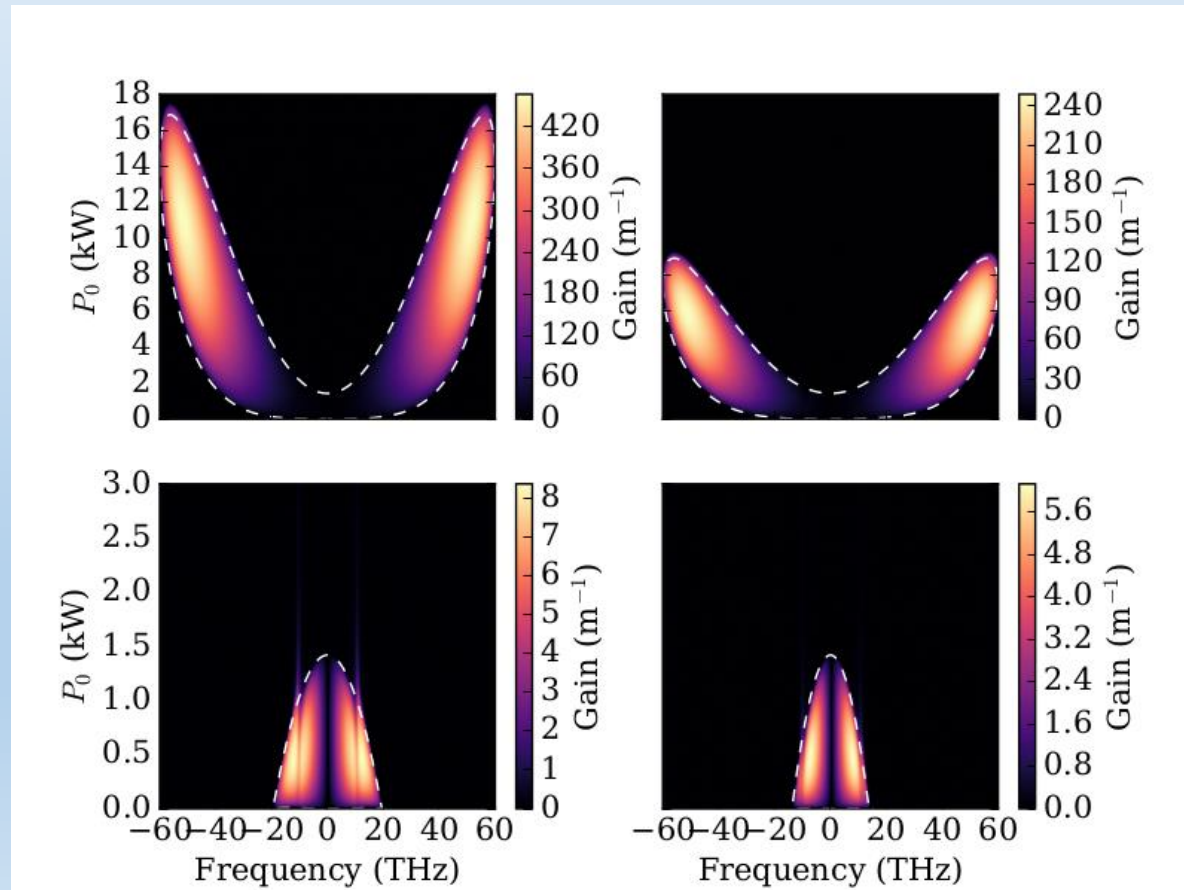
- In the absence of Raman scattering, there is a limit in the MI gain due to self-steepening (Shukla & Rasmussen, Opt. Lett., 1986, De Angelis et al., JOSA B, 1996)
- In general, the MI gain vanishes whenever the power is equal to

$$P_{\pm} = \hat{P}(\Omega) \times \left( 1 \pm \sqrt{1 - \tau_{sh}^2 \Omega^2} \right)$$

$$\hat{P}(\Omega) = -\frac{\widetilde{\beta}_e(\Omega)}{\gamma_0 \tau_{sh}^2 \Omega^2}$$

# Modulation instability: Power cutoff

- In the absence of Raman scattering, there is a limit in the MI gain due to self-steepening



- ✓ MI gain versus pump power
- ✓  $\beta_2 = -1 \text{ ps}^2/\text{km}$
- ✓  $\beta_4 = -16, -8, +8, +16 \times 10^{-4} \text{ ps}^4/\text{km}$
- ✓  $\gamma_0 = 100 \text{ 1}/(\text{W km})$
- ✓  $\lambda_0 = 5 \text{ }\mu\text{m}$

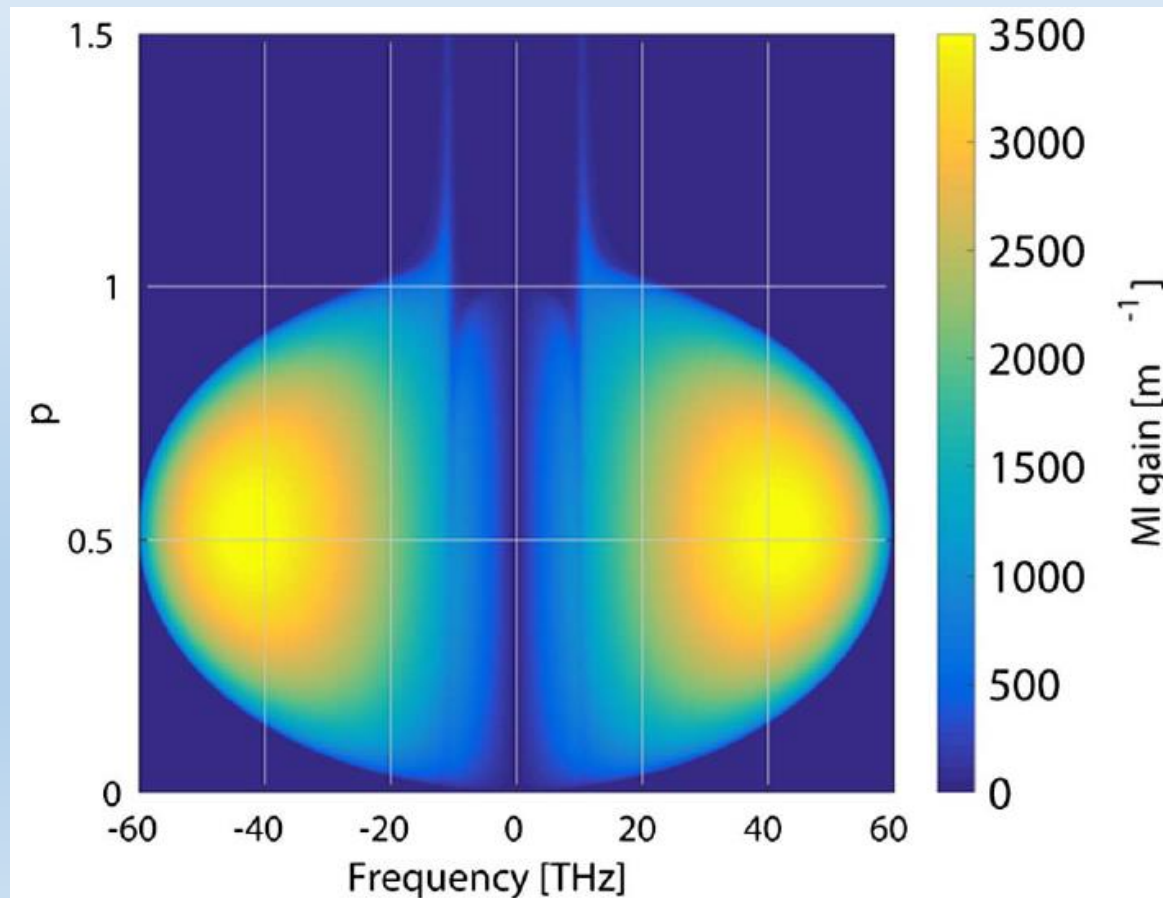
- Gain region
- Location of the maximum MI gain



Hernandez et al., IEEE Photonics J., 2017

# Modulation instability: Power cutoff

- In the presence of Raman scattering, there is still gain after the power cutoff



- ✓ MI gain versus normalized pump power
- ✓  $\beta_2 = -50 \text{ ps}^2/\text{km}$
- ✓  $\gamma_0 = 100 \text{ 1}/(\text{W km})$
- ✓  $\lambda_0 = 5 \text{ }\mu\text{m}$

Sánchez et al., JOSA B, 2018

# Tunable Raman gain

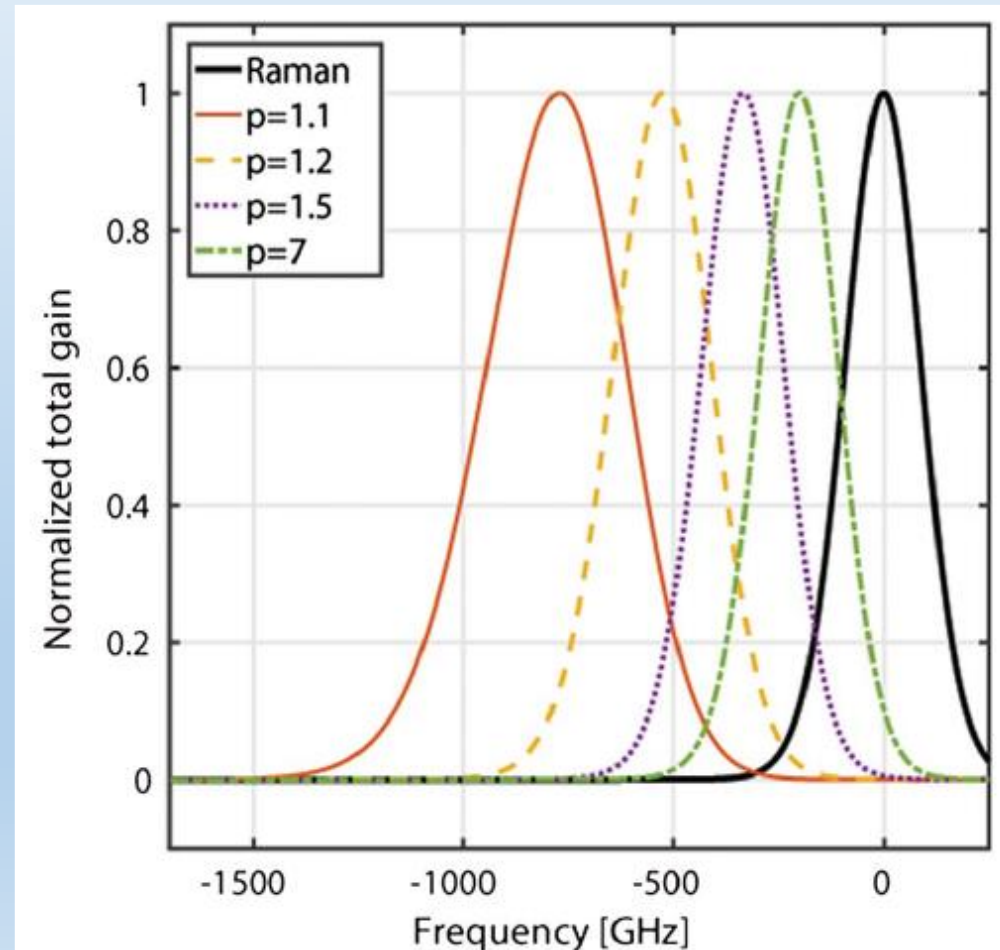
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- Gain beyond the cutoff power can be tuned using the pump power
- Possible applications
  - Mid-IR fiber Raman lasers
  - Mid-IR supercontinuum generation
- Why mid-IR?
  - Cutoff power  $\propto \tau_{sh}^{-2}$  and  $\tau_{sh} \approx \omega_0^{-1}$



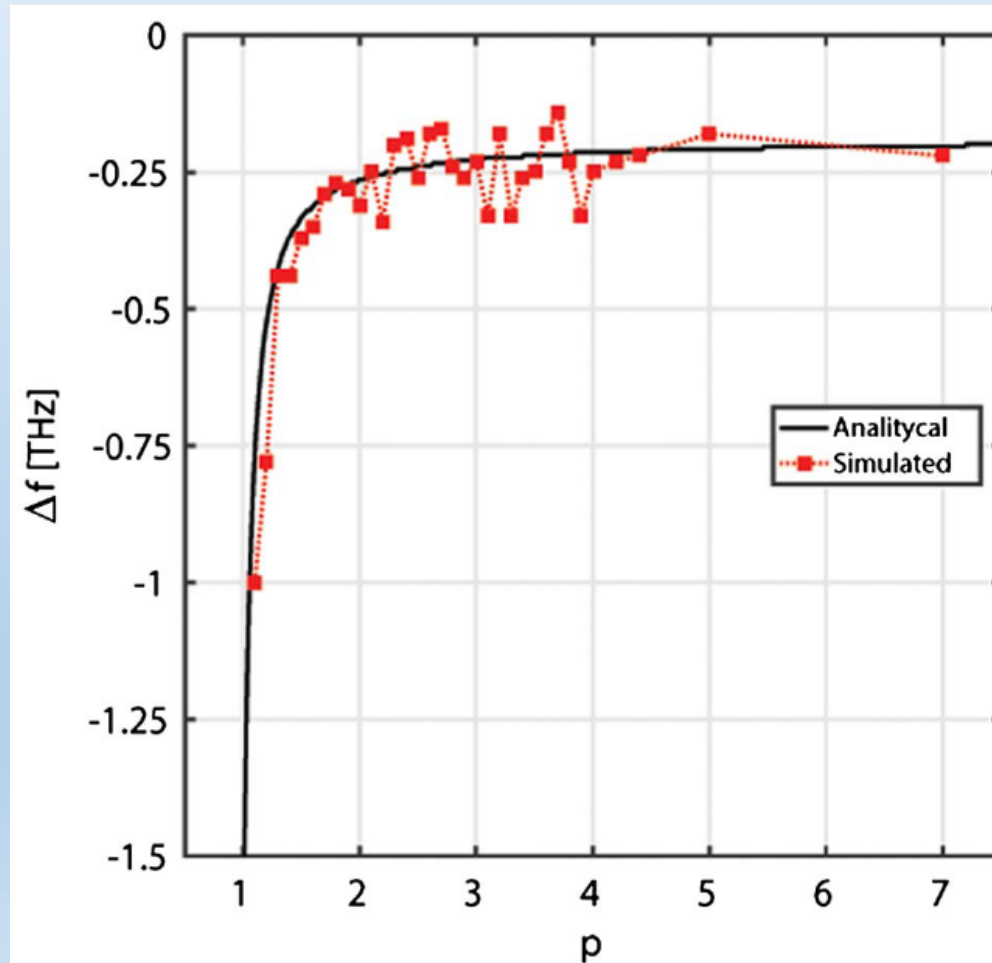
# Tunable Raman gain

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# Tunable Raman gain

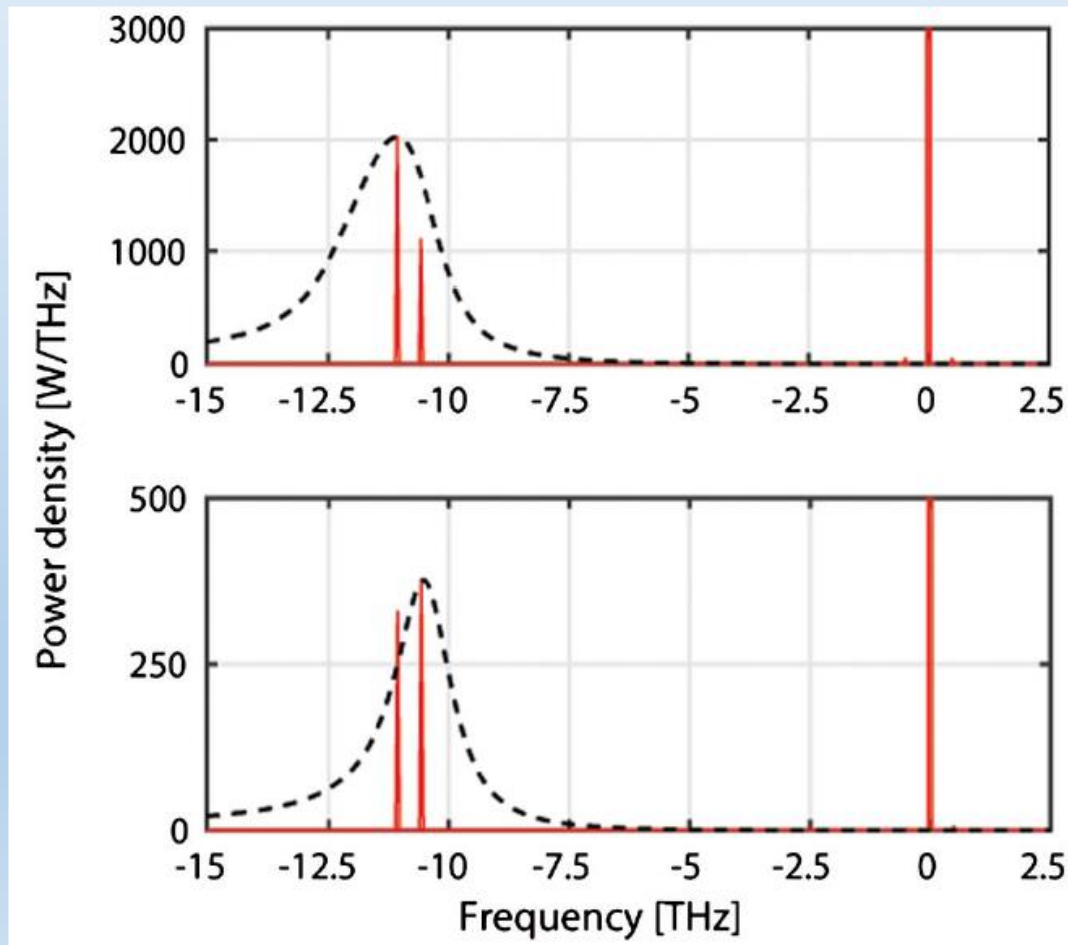
- Gain beyond the cutoff power can be tuned using the pump power



- ✓ Central frequency (deviation from Raman peak) as a function of the normalized power

# Tunable Raman gain

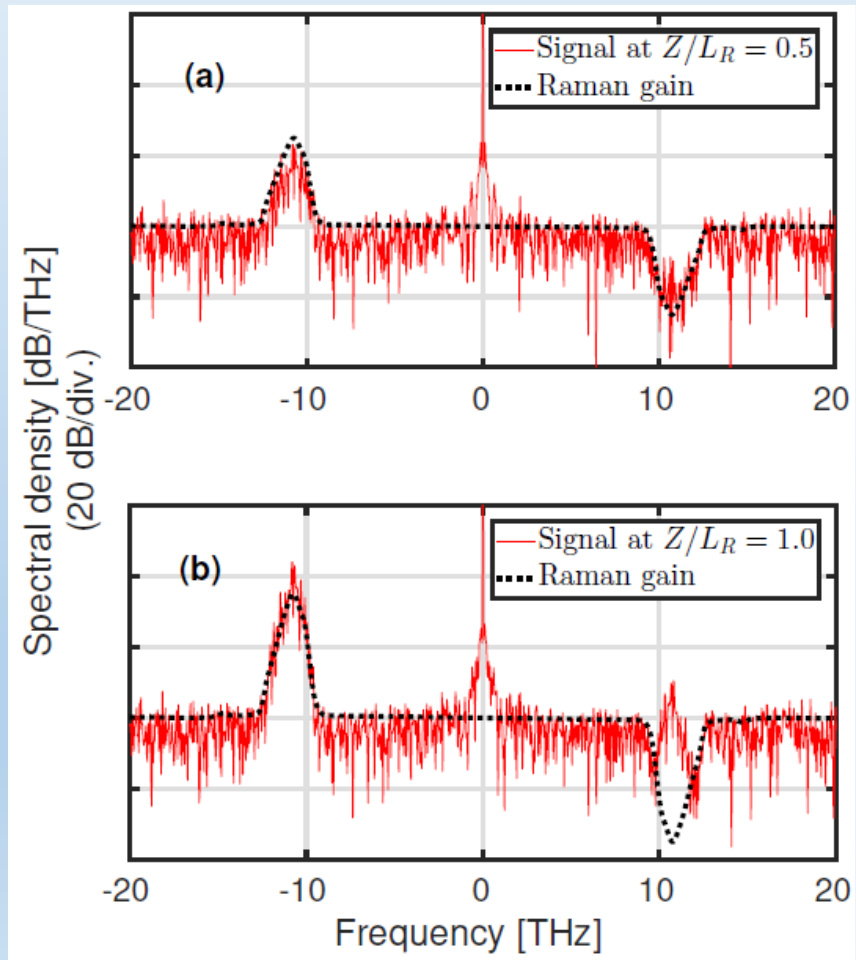
- Tuning a filter central frequency



- ✓ Same pump and two seeds (simulations)
- ✓  $p = 1.1$  (top) and  $p = 3.0$  (bottom)
- ✓ Output spectra after 3.6 mm

# Anti-Stokes Raman gain

- Raman gain appears only in the Stokes side of the pump (lower frequencies)

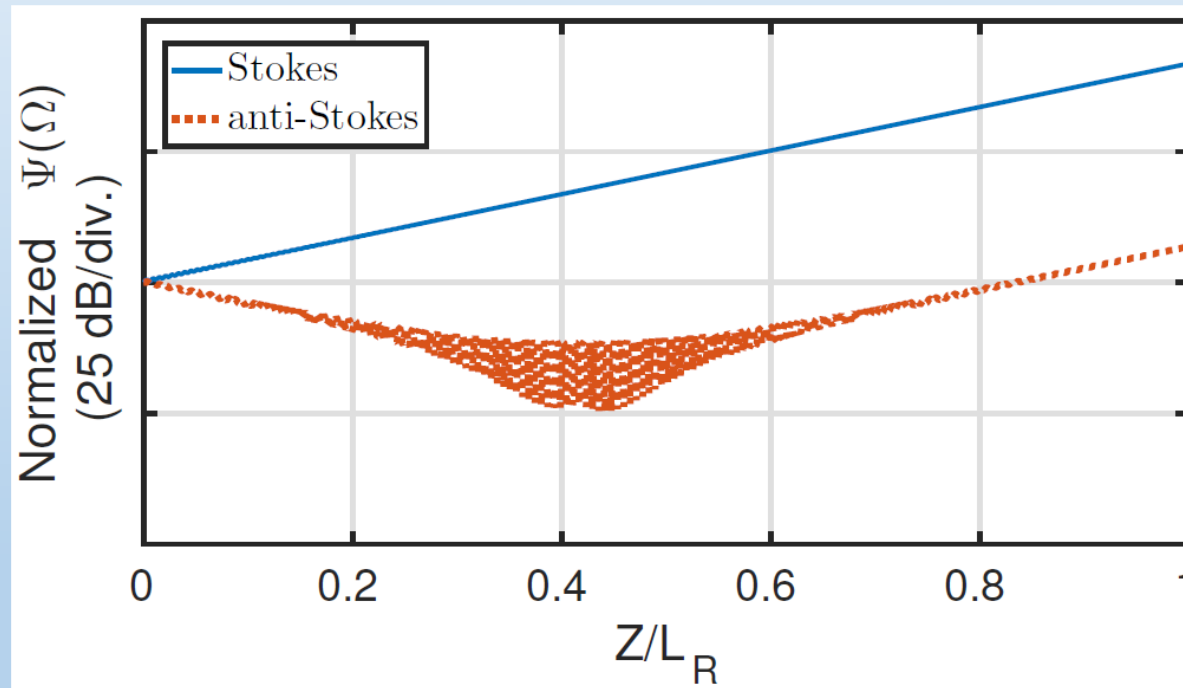


- ✓ CW pump + noise (simulations)
- ✓ Normal regime:  $\beta_2 = +50 \text{ ps}^2/\text{km}$
- ✓  $\gamma_0 = 100 \text{ 1}/(\text{W km})$
- ✓  $\lambda_0 = 5 \text{ }\mu\text{m}$

- Initially, there is no gain in the Stokes side
- Gain in the Stokes side appears as a consequence of four-wave mixing

# Anti-Stokes Raman gain

- Raman gain appears only in the Stokes side of the pump (lower frequencies)



- ✓ CW pump + seeds (simulations)
- ✓ Normal regime:  $\beta_2 = +50 \text{ ps}^2/\text{km}$
- ✓  $\gamma_0 = 100 \text{ 1}/(\text{W km})$
- ✓  $\lambda_0 = 5 \text{ }\mu\text{m}$

- Photon number is a conserved quantity

Sánchez et al., JOSA B, 2018 B

# Anti-Stokes Raman gain

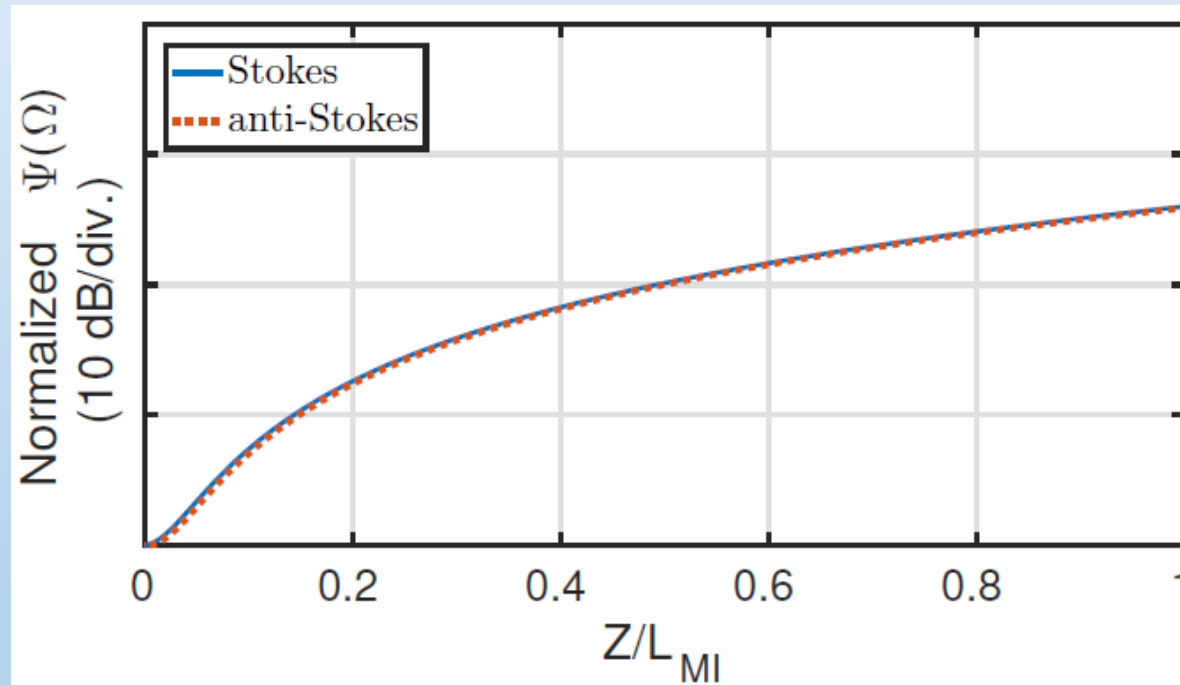
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- Raman gain appears only in the Stokes side of the pump (lower frequencies)
- However, in the case of tunable Raman gain, it appears also in the anti-Stokes band (higher frequencies)
- Both gain sidelobes are Raman-shaped
- It is a pseudo-parametric gain

Sánchez et al., JOSA B, 2018 B

# Anti-Stokes Raman gain

- Raman gain appears only in the Stokes side of the pump (lower frequencies)



- ✓ CW pump + seeds (simulations)
- ✓ Anomalous regime:  $\beta_2 = -50 \text{ ps}^2/\text{km}$
- ✓  $\gamma_0 = 100 \text{ 1}/(\text{W km})$
- ✓  $\lambda_0 = 5 \text{ }\mu\text{m}$
- ✓  $p = 1.1$

- Both seeds grow simultaneously

Sánchez et al., JOSA B, 2018 B

# Characterization of Raman

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- Raman delayed response

$$\frac{\partial A}{\partial z} - i\hat{\beta}A = i\hat{\gamma}A(z, T) \int_{-\infty}^{+\infty} R(T') |A(z, T - T')|^2 dT'$$

$$R(T) = (1 - f_R)\delta(T) + f_R h(T)$$

- $h(t)$  can be estimated from the Raman gain ( $\propto f_R n_2 \text{Im}\{\tilde{h}(\Omega)\}$ ) and using the Kramer-Kronig relations
- $f_R$  can be estimated given independent measurements of the Raman gain and  $n_2$



# Characterization of Raman

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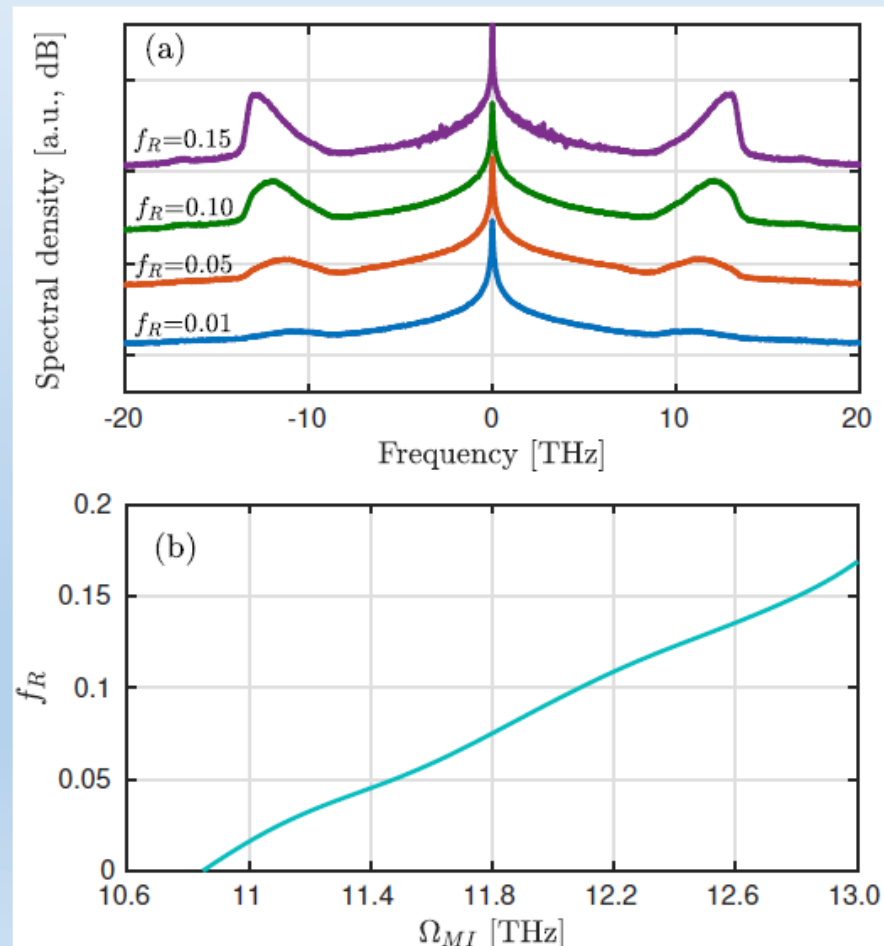
- Raman delayed response

$$R(T) = (1 - f_R)\delta(T) + f_R h(T)$$

- $f_R$  can also be estimated from independent measurements of the Raman gain and the differential scattering cross-section
  - This approach was used in Stolen et al., JOSAB, 1989, to fix the value  $f_R = 0.18$  used for silica fibers
- Time-resolved Z-scan can be used to measure both  $f_R$  and  $h(t)$ 
  - Error > 25% for  $f_R$  (Smolorz et al., J. Non-Crystalline Solids, 1999)

# Characterization of Raman

- Raman gain beyond the cutoff power enables another path to estimate  $f_R$



- The position of the peak of the Raman gain depends  $f_R$  ( $p = 10$ )
- Equations relating the position of the peak with  $f_R$



Sánchez et al., Opt. Lett, 2019

# Extension of the GNLSE

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- The Generalized Nonlinear Schrödinger Equation (GNLSE) does not preserve the photon number when a general nonlinear coefficient  $\tilde{\gamma}(\Omega)$  is used
- Waveguides based on new metamaterials require the use strongly frequency-dependent  $\tilde{\gamma}(\Omega)$ : some waveguides present a zero-nonlinearity wavelength
- We developed a new extension to the GNLSE that is physically meaningful and can model the propagation in new materials

Bonetti et al., JOSA B, submitted  
Bonetti et al., arXiv, 2019.

# Extension of the GNLSE

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- Following a quantum mechanical approach, the equation can be derived (dispersionless case) from the mean evolution of the Schrödinger equation (Lai & Haus, Phys. Rev. A, 1989)

$$\frac{\partial}{\partial z} |\psi\rangle = i\hat{H}|\psi\rangle$$

$$\hat{H} = \iiint \frac{\kappa}{2} \hat{a}_{\omega_1}^\dagger \hat{a}_{\omega_2}^\dagger \hat{a}_{\omega_1 - \mu} \hat{a}_{\omega_2 - \mu} d\omega_1 d\omega_2 d\mu$$

- $\hat{A}_\omega \propto \hat{a}_\omega \sqrt{\omega_0 + \omega}$
- $\kappa$  is related to the third order susceptibility
- Restriction on frequency dependence: hermiticity requires  $\kappa_{\omega_1, \omega_2, \omega_3, \omega_4} = \kappa_{\omega_4, \omega_3, \omega_2, \omega_1}^*$

# Extension of the GNLSE

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- Hard-to-conduct measurements of the four-frequency dependence
- Idea: use generalized Miller's rule

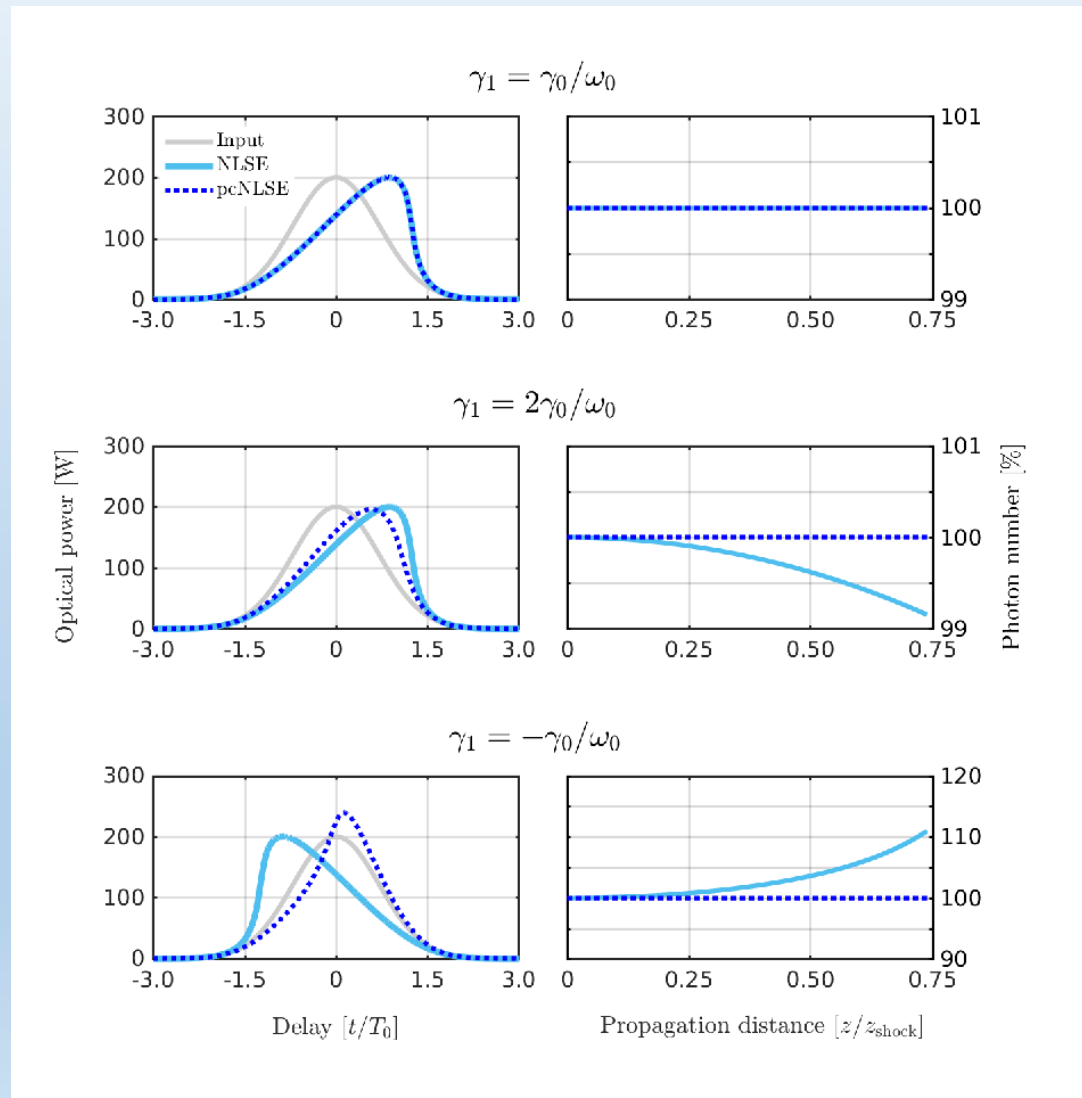
$$\chi_{\omega_1, \omega_2, \omega_3, \omega_4}^{(3)} \propto \chi_{\omega_1}^{(1)} \chi_{\omega_2}^{(1)} \chi_{\omega_3}^{(1)} \chi_{\omega_4}^{(1)}$$

- Motivated by this idea:

$$r_{\omega} \propto \sqrt[4]{\gamma(\omega) \times (\omega_0 + \omega)}$$

$$\kappa_{\omega_1, \omega_2, \omega_3, \omega_4} = \text{Re}(r_{\omega_1} r_{\omega_2} r_{\omega_3} r_{\omega_4})$$

# Extension of the GNLSE



- ✓ 100 ns pulse
- ✓ Dispersionless
- ✓  $\gamma_0 = 1.2 \times 10^{-3} \text{ 1/(W km)}$
- ✓  $\lambda_0 = 1550 \text{ nm}$
- ✓  $P_0 = 200 \text{ W}$

# Summary

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- Analytical expressions for the initial stage of MI in the pump+noise case
- Higher-order perturbation solution beyond the first-order linear solution
- Study of the pump power limits of the MI gain
- Tunable Raman (both Stokes and anti-Stokes bands) beyond the pump cutoff power
- A method to measure the fractional Raman gain  $f_R$
- Extension to the GNLSE that allows to model propagation in new materials

# Ongoing work

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- Extension of the GNLSE, valid for new materials, that includes Raman
- Parametric processes in bulk nonlinear crystals, such as GaSe and AgGaSe<sub>2</sub>, with a second order nonlinear susceptibility  $\chi^2$ 
  - Generation of pairs of correlated photons for quantum information transmission



Thank you!

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# References: Nonlinear optics

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- D. F. Grosz, S. M. Hernandez, and P. I. Fierens, “*Supercontinuum Generation and Rogue Waves in the mid IR*”, Invited Talk, Extreme Events in Complex Optical Systems (EECOS), 1-4 December 2015, Buenos Aires, Argentina.
- P. I. Fierens, S. Hernandez, J. Bonetti, and D. F. Grosz, “*On the spectral dynamics of noise-seeded modulation instability in optical fibers*”, International Conference on Applications of Nonlinear Dynamics (ICAND), 28 August -1 September 2016, Denver, Colorado, EE.UU.
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